

Slope of a Line

The **slope** of a line is the measure of the **inclination** of the line.



Slope Formula

Determine the missing coordinates in the following points, given the slope of the line between them.

- a) The slope between the point A(2, 7) and B(5, y) is $\frac{4}{3}$.
- b) The slope between the point C(8, 12) and D(x, 7) is -5.

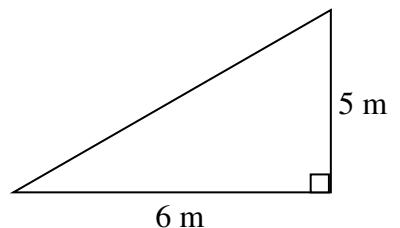
2

Determine the slope of the line that passes through the following points.

a) A (3,2) and B (7,1)

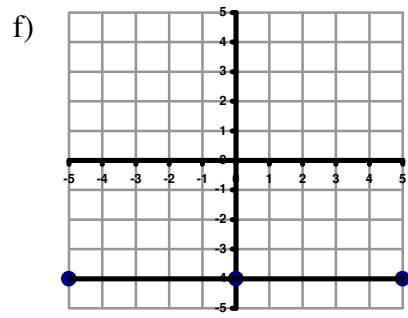
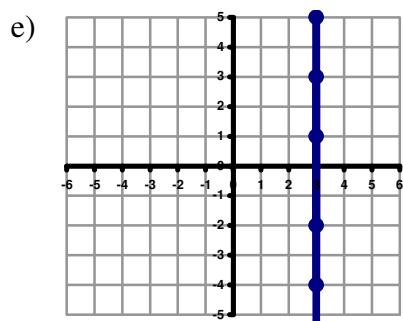
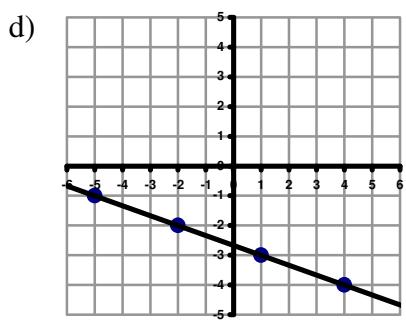
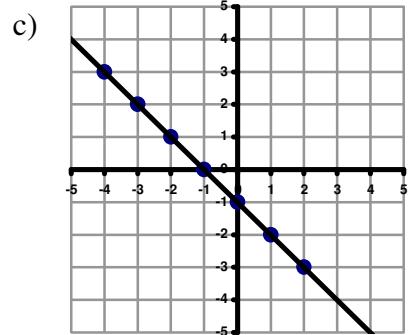
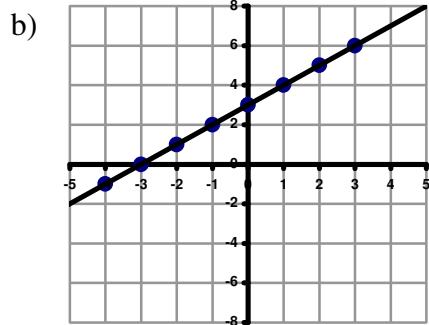
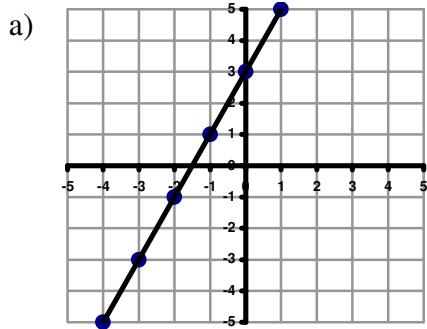
b) G (7,-3) and H (-2,-5)

c)



3

Determine the slope of each of the following lines.



Determine the missing coordinates in the following points, given the slope of the line between them.

- a) The slope between the point A(2, 7) and B(5, y) is $\frac{4}{3}$.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\frac{4}{3} = \frac{y-7}{5-2}$$

$$\frac{4}{3} = \cancel{\frac{y-7}{3}}$$

$$12 \stackrel{+21}{=} 3y - 21 \stackrel{+21}{=}$$

$$33 \stackrel{\div 3}{=} 3y \stackrel{\div 3}{=}$$

$$\boxed{11 = y}$$

- b) The slope between the point C(8, 12) and D(x, 7) is -5.

$$\begin{array}{|c|c|} \hline x & y \\ \hline 8 & 12 \\ \hline x & 7 \\ \hline \end{array} \quad m = \frac{\Delta y}{\Delta x}$$

$$7-12 = -5$$

$$\frac{-5}{1} \cancel{\times} \frac{-5}{x-8}$$

$$\begin{aligned} -5x + 40 &= -5 \\ -5x &\stackrel{\div(-5)}{=} -45 \\ x &= 9 \end{aligned}$$

The Slope of a Line

The slope of a line measures how steep the line is (angle of inclination).



Slope Formula

$$m = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

2

Determine the slope between each set of points (and diagram) below.

a) A (3, 2) and B (7, 1)

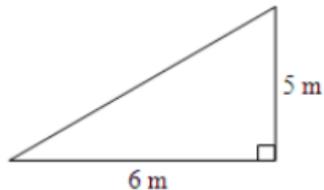
$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{1 - 2}{7 - 3} \\ &= \frac{-1}{4} \end{aligned}$$

b) G (7, -3) and H (-2, -5)

$$\begin{array}{c|c} x & y \\ \hline 7 & -3 \\ -2 & -5 \end{array}$$

$m = \frac{\Delta y}{\Delta x} = \frac{-2}{-9} = \frac{2}{9}$

c)

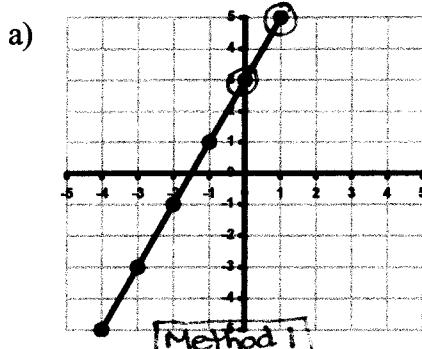


$$\begin{aligned} m &= \frac{\text{rise}}{\text{run}} \\ m &= \frac{5}{6} \end{aligned}$$

Slope Formula

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

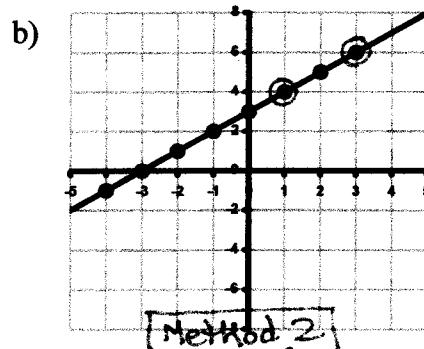
3) Determine the slope and y-intercept of each of the following lines:



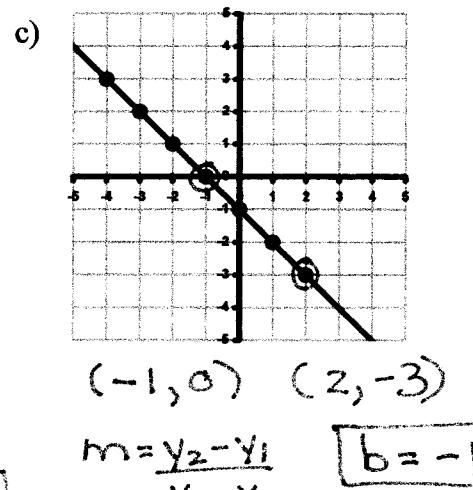
$$+1 \begin{pmatrix} 0 \\ 3 \end{pmatrix} + 2 \begin{pmatrix} 1 \\ 5 \end{pmatrix} \quad m = \frac{2}{1}$$

$m = 2$

$y\text{-int} = 3$



$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad b = 3$$

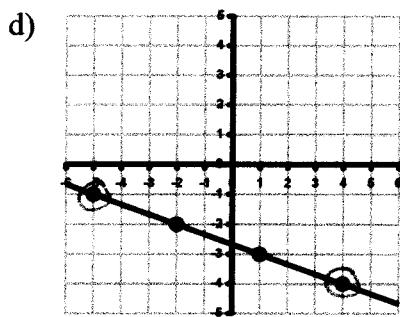


$$m = -1$$

$$m = \frac{-3 - 0}{2 - (-1)}$$

$$m = \frac{-3}{3}$$

$$m = -1$$



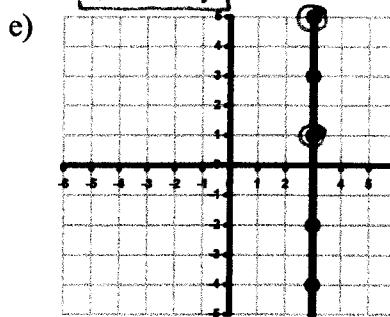
$$(-5, -1) \quad (4, -4)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-4 - (-1)}{4 - (-5)} = -\frac{3}{9} = -\frac{1}{3}$$

$$m = \frac{-4 - (-1)}{4 - (-5)} = -\frac{3}{9}$$

$$m = \frac{-4 + 1}{4 + 5} = -\frac{3}{9}$$

$$m = -\frac{1}{3}$$



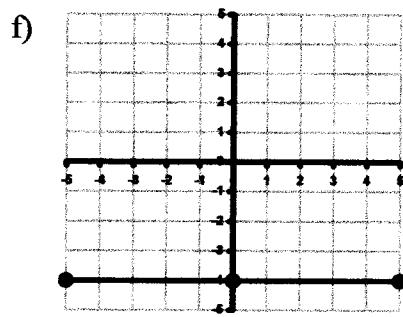
$$(3, 1) \quad (3, 5)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{5 - 1}{3 - 3} = \frac{4}{0}$$

$$b = \text{None}$$

Undefined
or
 $m = \infty$



$$(0, -4) \quad (5, -4)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{-4 - (-4)}{5 - 0} = \frac{0}{5} = 0$$

$$m = 0$$

$$b = -4$$

* Use your favourite method*