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Derivative Worksheet #1

Find the derivative of the following functions:

1. $f(t) = 7t - 12$

2. $f(x) = 6$

3. $f(x) = 12x^4 + 3x^2 + 7$

4. $y = -6x^3 + 5x^2 - 8x + 2$

5. $d(t) = 360 + 40t - 16t^2$

6. $g(t) = 7t^4 - 4t^3 + 6t^2 + 9t - 19$

7. $y = 2 - 4x + 7x^2 - 9x^3$

8. $f(x) = 0$

9. $f(x) = e^x$

10. $f(x) = e^2$

11. $f(t) = (t + 2)(t - 1)$

12. $y = (2x + 1)(3x + 4)$

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Derivative Worksheet #2

Find the derivative of the following functions using product/quotient rules:

$$1. \quad f(t) = (7t - 12)(4t^3)$$

$$2. \quad f(x) = 6(7x - 3)(2x^2)$$

$$3. \quad f(x) = (2x^4 + 3x^2 + 7)(9 - x^3)$$

$$4. \quad y = -(6x^3 + 5x^2 - 8x + 2)(4 - x)$$

$$5. \quad d(t) = (4t)(10 - 4t)$$

$$6. \quad g(t) = (7t^4 - 4t^3)(6t^2 + 9t - 19)$$

$$7. \quad y = (2 - 4x) / (x^2 - 3x^3)$$

$$8. \quad f(x) = (2 - 3x + 5x^2 - 8x^3) / 9$$

$$9. \quad f(x) = e^x / x$$

$$10. \quad f(x) = e^2 / x^4$$

$$11. \quad f(t) = (6t + 2) / (7t - 1)$$

$$12. \quad y = (2x + 1) / (3x + 4)$$

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Product & Quotient Rule Practice:

1. $\frac{d}{dx} (x^3 - 2x + 1)(x^4 + x - 3)$

2. $\frac{d}{dx} \left(\frac{x^2 + 1}{x^2 - 1} \right)$

3. $\frac{d}{dx} \left(\frac{x^2}{\sin x} \right)$

4. $\frac{d}{dx} (\sin x \cos x)$

5. $\frac{d}{dx} (\sin^2 x)$

6. $\frac{d}{dx} \left(\frac{x+1}{\sqrt{x}} \right)$

7. $\frac{d}{dx} \left(\frac{1+\sin x}{1-\cos x} \right)$

8. $\frac{d}{dx} (\sqrt{x} e^x)$

9. $\frac{d}{dx} \left(\frac{e^x}{1+x} \right)$

10. $\frac{d}{dx} (2^x e^x)$

11. $\frac{d}{dx} \left(\frac{3^x}{x+1} \right)$

12. $\frac{d}{dx} \left(\frac{x^2 - x - 2}{x+1} \right)$

13. Find the equation of the tangent line to the curve $y = \frac{\sqrt{x}}{x+1}$ at $x=4$

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Chain Rule Practice

1. $\frac{d}{dx} \cos(x^2)$

2. $\frac{d}{dx} \sqrt{1 + \frac{1}{x}}$

3. $\frac{d}{dx} \left(3 + (x^3 - 2x)^5 \right)^8$

4. $\frac{d}{dx} \tan^3 \sqrt{x}$

5. $\frac{d}{dx} \sqrt{x^3 + 6x}$

6. $\frac{d}{dx} \sec(x^2)$

7. $\frac{d}{dx} \sec^2 x$

8. $\frac{d}{dx} \cos^3(x^2)$

9. $\frac{d}{dx} \sin 2x \cos 3x$

10. $\frac{d}{dx} x^2 \cos e^x$

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PRACTICE 1 - Implicit Differentiation

Find $\frac{dy}{dx}$:

1. $y^3 + 7y = x^3$

2. $4x^2y - 3y = x^3 - 1$

3. $x^2 + 5y^3 = x + 9$

4. Find $D_t y$ if $t^3 + t^2y - 10y^4 = 0$

5. Find the equation of the tangent line to the curve $y^3 - xy^2 + \cos(xy) = 2$ at $x = 0$.

6. Find $\frac{d^2y}{dx^2}$ at $(2,1)$ if $2x^2y - 4y^3 = 4$.

7. Find the equation of the normal line (line perpendicular to the tangent line) to the curve $8(x^2 + y^2)^2 = 100(x^2 - y^2)$ at the point $(3,1)$.

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PRACTICE 2 - Implicit Differentiation

Compute $\frac{dy}{dx}$ for the problems below:

1. $x^2 + y^2 = 1$

2. $x^2 - \frac{1}{2}y^2 = 1$

3. $2x^3y^2 + 2 = 4x$

4. $x^4y^4 + 3x^2y^2 = 1$

5. $5xy + 3x^2 = 4y^2$

6. $(x + y)^2 = 4xy$

7. $e^{xy} + xy = 3x^2$

8. $\ln(x^2 + y^2) = y^3$

9. $\frac{x+y}{xy} + 2x = \frac{1}{5}y^5$

10. $\frac{x}{y} + \frac{y}{x} = e^{x^2+2xy+y^2}$

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PRACTICE 3 - Implicit Differentiation

1. Differentiate each expression, treating y as a function of x . (If you cannot differentiate single expressions accurately, you certainly cannot use implicit differentiation on equations.)

(a) $\frac{d}{dx} 5y^3 =$

(b) $\frac{d}{dx} (7x^5 + 2y^5) =$

(c) $\frac{d}{dx} \sin(2y - e^x) =$

(d) $\frac{d}{dx} (\ln(3x + 2y)) =$

(e) $\frac{d}{dx} x^3 y^7 =$

(f) $\frac{d}{dx} e^{(3x + 5y)} =$

(g) $\frac{d}{dx} (7y + e^{5y}) =$

(h) $\frac{d}{dx} (\ln(3+y) + \cos(2y) + \ln(5)) =$

2. Use Implicit Differentiation on each equation to find $\frac{dy}{dx}$ (or y')

(a) $5x^3 + 2y^5 = 7 + y^2 + 3x$

(b) $x^3 + 2y^3 = 7y + 5x + 4$

(c) $\ln(3+y) + \cos(5x) = e^y + x^2$

(d) $xy + \cos(2y) = \ln(7-x^3) + 7^x + 3$

(e) $\tan(2+5y^2) + x^2 y^3 = \ln(3+y)$

(f) $e^{3x} + \sin(5y) = y^3 + x^5 + 4$