NOTESsomeANS

Notes that are done in class will be updated online periodically

(Any questions left blank you are responsible) to my yourself -> get help if needed.

1 1 11 n	i+ 6	11U C D	ate.	Name:					
1101	11.0	IIIOC D	atc						
	Tentati	ve TEST	「 date	Sinusoidal Functions Unit					
	Reflect – previous TEST mark, Overall mark now Looking back, what can you improve upon?								
?	In this function propert	unit you ns are ca ties to sk ou will le	will learn alled sinu etch thes	ng Goals how trigonometry can be used to model wavelike relationships. The usoidal functions. You will study key properties of the sine function as functions, to model real life situations and to solve problems. If you the cosine function is very similar to sine function, however the tange	and use these I go on studying				
Fig.	Succ	ess C	riteria	1					
X		I am re	ady for th	nis unit if I am confident in the following review topics ood at & review the ones you left undrolled before you get too far behind) graphs, simplifying expressions, solving equations, transformations, function notation,	domain & range				
				e <u>new topics</u> for this unit if I can do the practice questions in the textbo	ook/handouts				
		(cneck on tr	Date	Topics	Done?				
				CBR Investigation of Motion Handout & EXTRA "Roll the Shape" Experiment					
				Periodic Behaviour					
				Section 6.2 p331 #4,5,6,7,8 & EXTRA Handout Sine Function Investigation					
				Section 6.3 p339 #1,3,4,6,7,9 & EXTRA Handout					
				Comparing Sinusoidal Functions Section 6.4 p348 #3,4,5,6,7					
				Translating/Shifting the Sine Function Section 6.5 p365 #3,4,6,9,11					
				Stretching/Compressing the Sine Function Section 6.6 p375 #13,15,17,19 & Extra Handout					
				one EXTRA group Activity – if there is time one EXTRA Handout on KU APP COMM TIPS					
		l am <u>pr</u>	epared f	or the test/evalutation if					
			lunders	stand the main concepts from each lesson					
			:	if not, ask other students in class to help you study or visit the peer tutoring room or ask the teacher for help or get also practice "knowledge-understanding" questions from the textbook – look for questions marked by sc	a private tutor				
			I can ex	plain/communicate the ideas clearly					
		_	l can ar	If not, practice explaining a solved question to someone else or complete the assigned journal questions also practice "communication" questions from the textbook – look for questions marked by a oply these concepts in word problems					
		_	I did no	trinot, practice "application" questions from the textbook – look for questions marked by A t just memorize steps to do for different types of questions, I understa sincept and therefore can do problems in new contexts	nd the ideas behin				
			•	If not, practice "thinking-inquiry-problem-solving" questions from the textbook – look for questions marked by $ au$ o questions independently					
			l can co	if not, try redoing an already solved example without looking at solutions omplete questions quickly and with confidence					
			l compl	if not, try timing yourself for similar type questions to see progress eted the review and/or practice test					

Corrections for the textbook answers:

CBR Investigation of Motion

🔯 The Calculator Based Ranger - CBR is a distance sensor that acts much the same as a submarine or bat to determine its location with respect to an object (it sends out sound waves then determines the time it takes for them to hit the object and bounce back, thus giving its location, or distance from the CBR).

(get program to work between calc and ranger) Calc: 2nd, Link, -> , Enter CBR Set-up:

ranger: 82/83

(get into program) Program, Ranger, Enter

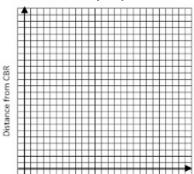
(get sample) Set up, up, start now, ... repeat sample (matching graphs) Applications, meters, dist.match

Instructions:

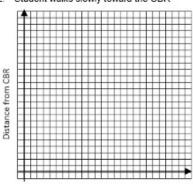
create a clear area for walking in front of CBR, hold a flat surface(ie book) in front yourself as you walk, walk steady, ignore jumps in the graph, the instrument is not very precise.

Sketch the graph first, then walk, then compare if your prediction was correct.

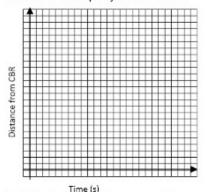
Student walks slowly away from CBR



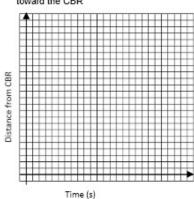
2. Student walks slowly toward the CBR



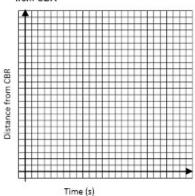
3. Students walks quickly toward the CBR



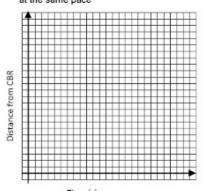
Student increases speed while walking toward the CBR



Student decreases speed while walking away

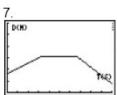


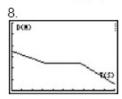
6. Student walks away from ranger, at 2 meters stops for 5 seconds, then returns at the same pace

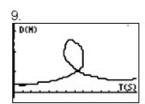


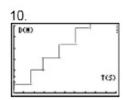
Do some match the graph activities on the CBR for practice, then answer the following questions.

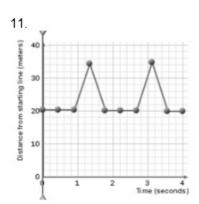
Describe how to create or explain why it is impossible to create the following graphs.

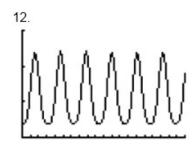




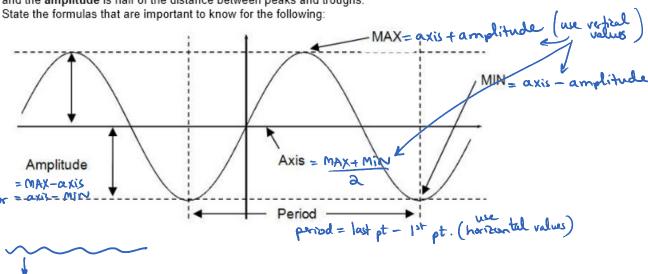




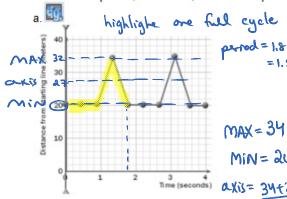


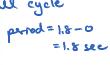


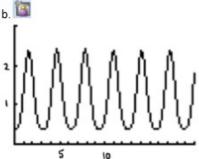
The last two graphs are examples of periodic motion, since they repeat in exact same cycles. A cycle is a series of events that are regularly repeated, a complete set of changes, starting from one point and returning to the same point in the same way. The period is the interval of the independent variable (usually time) needed for one complete cycle. Peaks



13. Find the period, max& min, axis and amplitude of the these periodic functions.







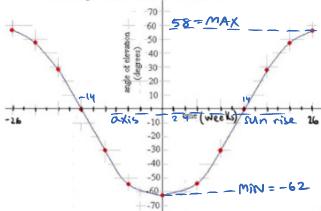
Time (seconds)
$$axis = 34+20 = 54 = 27$$

14. What real life relationships can be represented by periodic functions?

Periodic Behaviour

There are many situations in real life that reapeat in cycles. For example, ocean tides, daylight hours, average temperature for the year, heartbeat, volume of air in lungs, rides on ferris wheels, pendulum swings, frequency of musical notes, the list can go on.

After the sun rises, its angle of elevation increases rapidly at first, then more slowly, reaching a maximum in 26 weeks. Then the angle decreases until sunset.



When does sunrise occur at this time of the year, for this particular spot on Earth?

after 14 weeks (North pole has ± year day)
this maybe somewhere close to
North / South poles What is the period? What is longer the night or the day for this situation?

Night = 28 weeks perN=26+26=52 weeks Day = 24 weeks ... Night is longer

c. What is the axis? amplitude? range?

axis =
$$58+-62$$
 amplitude = 60°
= -2° Ronge $90 + 10^{\circ}$ Ronge $90 + 10^{\circ}$

d. Extrapolate the angle of elevation in tweeks and read beyond given data read within given data

(30) = 48

0(W)

8(20) = 28°

e. During what times is the angle of elevation of the sun above 30 degrees?

approximately between

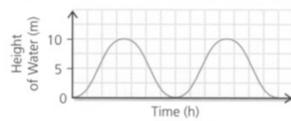
30° at -20 weeks -> add period = 52

to have positive

and 20 weeks " between 20 weeks and 32 weeks

the sun is higher than 300

The Bay of Fundy, which is between New Brunswick and Nova Scotia, has the highest tides in the world. There can be no water on the beach at low tide, while at high tide the water covers the beach.



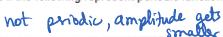
Why can you use periodic functions to model the

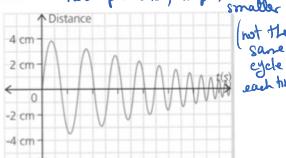
b. What is the change in depth of water from low tide to high tide?

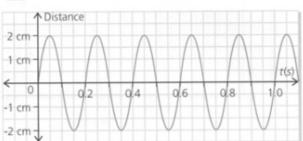
Determine the equation of the axis of the curve.

What is the amplitude of the curve?

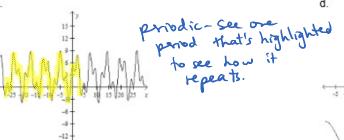
3. Determine if the following represent periodic functions or not.

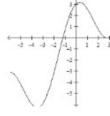






C.





- e. Dependent = the horizontal distance travelled by the grandfather clock's pendulum
- f. Dependent = cost of riding a taxi Independent = distance travelled

Independent = time

periodic/repeats The same way all the time

g. Dependent = interest on the money invested at 5% Independent = principal deposited

Not periodic (Linear)

h. Dependent = the height of the pedal on a moving bicycle Independent = minutes

i.	x	у	
check ? x values ore m order	-3	7	x4M
x values	1	4	
ore m	5	1	MiM
	9	4	
+ same	13	7	MAX
count	17	4	
~	21	1	MIN

j.	х	у	_
	0	-2	_
	2	3	_
	4	0	_
	6	-2	
	8	-4	
	10	0	
	12	3	
			-

7 1	Hal	+ 5	11UC Date:	
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Sine Function Investigation



🔯 Introduction: In this investigation you are going to learn how the sine function you used to solve triangles in the last unit will relate to circular motion and how it creates wavelike graphs.

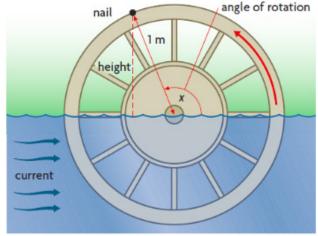
Equipment needed:

- Template of circle with degrees on it shown to be halfway submerged in water.
- Template of circle with a drawn nail on it to cut out
- Template of the ruler of the same size as the radius of the circle to cut out
- Cardboard to tape on it the circle submerged in water
- Thumbtack to pin the circle with nail to the centre of the circle submerged in water.
- Scientific calculator (with sin cos tan buttons)

Steve uses a generator powered by a water wheel to produce his own electricity.

- · Half the water wheel is below the surface of the river.
- The wheel has a radius of 1 m.
- The wheel has a nail on its circumference.

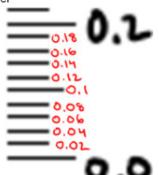
As the current flows, the wheel rotates in a counterclockwise direction to power the generator. The height of the nail, relative to the water level, as the wheel rotates is graphed in terms of the angle of rotation, x.



Performing the Experiment:

- 1. Tape the circle that is shown to be halfway submerged in water onto the cardboard
- 2. Cut out the other circle with the nail drawn on it and cut out the ruler along the edge.
- 3. Pin the centres of the circles together in such a way so that the top circle, with the nail on it, can rotate and so that the degrees on the bigger circle are still visible.
- Rotate the nail from the initial position at 0° to different degree measurements and record in the table below the heights of the nail above the surface of the water at these different angles.





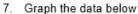
Observations:

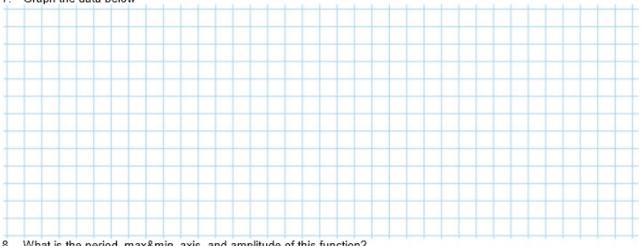
Angle	0	30	60	90	120	150	180	210	240	270	300	330	360	390	420	450	480	510
Height						2 0											0 0	

Name: _

Now	. Now use the calculator in degree mode to calculate:																	
Angle (x)	0	30	60	90	120	150	180	210	240	270	300	330	360	390	420	450	480	510
Sin(x)																		

6. What do you notice?





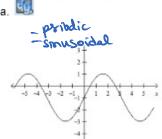
8. What is the period, max&min, axis, and amplitude of this function?

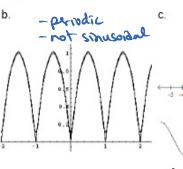
You will be studying sinusoidal functions - which are created by transforming (stretching/compressing, reflecting and shifting) this parent sine function. Identify the 5 key points on the graph of the parent sine function.

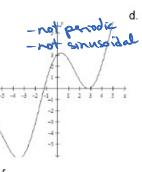


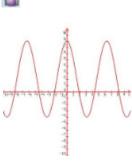
- 5 pomb:
- 1. First point
 2. Last point = 1st last Jaxis 5. Three Questes in = Min
 3. Middle point = 1st last Jaxis 5. Three Questes in = Min
- 10. Classify each as periodic or nonperiodic and sinusoidal or nonsinusoidal

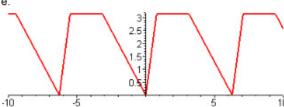


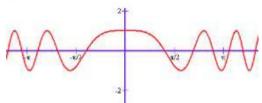












Comparing Sinusoidal Functions



Some of the questions in the textbook require you to graph with technology. There are lots of applets you can use online, or you can download a free program to use on your computer offline.

Online Graphing Calculator

http://my.hrw.com/math06 07/nsmedia/tools/Graph Calculator/graphCalc.html

Download GeoGebra (offline and online) http://www.geogebra.org/cms/en/download,

select webstart, for offline select appletstart, for online

Graphing technology often does not have degrees as independent variable. It has radians - which you will learn in gr.12 (if you go on studying math - college technology then advanced functions)

For now, if the equation has a degree symbol in it

set
$$k = \frac{\pi}{180^\circ}$$
 as a multiple of the given k value

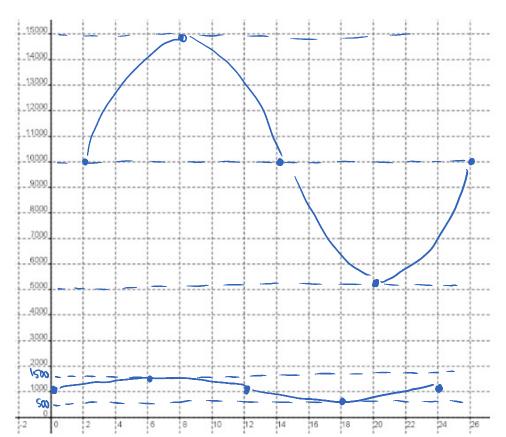
ex.
$$y=3\sin 5^{\circ}x-2$$

enter as $y=3\sin(5^{\circ}\cdot\frac{\pi}{180}x)-2$ to see graph in degrees



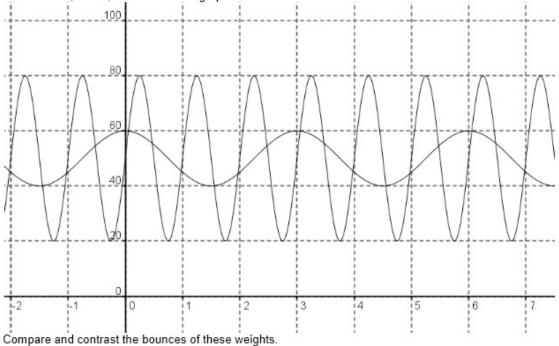
- 1. The population, F, of foxes in the region is modelled by the function $F(t) = 500 \sin(15t)^{\circ} + 1000$, where t is the time in months. The population, R, of rabbits in the same region is modelled by the function, $R(t) = 5000 \sin(15t - 30)^{\circ} + 10000$
 - a. Graph F(t) and R(t). Use technology to help you. From technology note where the cycle starts and ends on the axis, what the max and min values are, then use that information to sketch below:





•1

Two weights attached to the end of two springs are bouncing up and down. As they bounce their height, in cm, varies with time, in sec, as shown in the graph:

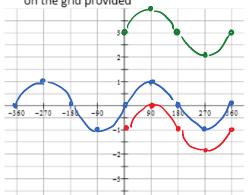


Start the homework practice in class.

Translating/Shifting the Sine Function ${\it y}$ = $\sin heta$

Part 1: Vertical Displacements (Up & Down)

1. On the graphing calculator, draw the functions $y = \sin \theta$, $y = \sin \theta + 3$, and $y = \sin \theta - 1$. Sketch the graphs below on the grid provided



STEPS USING THE GRAPHING CALCULATOR:

- Put the calculator in degree mode.
 Press MODE. Scroll down and across to DEGREE. Press
- ii. Adjust the window to correspond to the given domain. Use the following settings:

Xmin=-360 Xmax=360 Xscl=90 Ymin =-2 Ymax=4

- iii. Enter y = sin x into the equation editor. Press GRAPH. Enter remaining equations
- 2. Describe how the graphs of $y = \sin \theta$, $y = \sin \theta + 3$, and $y = \sin \theta 1$ are related.

 \sum 3. Summarize what the letter c represents in $y = \sin \theta + c$

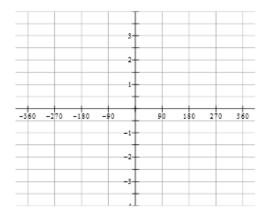
4. Fill in key characteristics of each graph.

	$y = \sin \theta$	$y = \sin \theta + 3$	$y = \sin \theta - 1$
axis	0	3	-(
Max&Min	MAX=1 MiN=-1	MAX=4 MIN=2	MAX=0 MM=-2
Period	360°	360°	360°
Amplitude		1	1
Where 1 st and last pts occur	14=0° Just=360°	1x=00 lost=360°	15=00 (ast= 360°

5. Out of all the properties (axis, Max&Min, period, amplitude, five points of cycle), which get affected by c?

Part 2: Phase Shifts (Left & Right)

6. On the graphing calculator, draw the functions $y = \sin \theta$, $y = \sin(\theta - 90^\circ)$, and $y = \sin(\theta + 180^\circ)$. Sketch the graphs below on the grid provided.



7. Describe how the graphs of $y = \sin \theta$, $y = \sin(\theta - 90^\circ)$, and $y = \sin(\theta + 180^\circ)$ are related.



8. Summarize what the letter d represents in $y = \sin(\theta - d)$

9. Fill in key characteristics of each graph.

	$y = \sin \theta$	$y = \sin(\theta - 90^{\circ})$	$y = \sin(\theta + 180^{\circ})$
axis			
Max&Min			
Period			
Amplitude			
Where 1 st and last pts occur			

10. Out of all the properties (period, Max&Min, axis, amplitude, five points of the cycle), which get affected by d?

- 11. Sketch and state the equation for the following then identify the period, axis, amplitude, range, domain for the first cycle.
- a. the sine function has been moved 39 units down and 23° to the left b. the sine function has been moved 30 units up and 58° to the right.

J=
$$\sin(0+23^\circ)-39$$

period = 360°

[st pt = -23°

axis = -39

last pt = -23°+360°=337°

amplitude = |

range fyell, -40±y=-38°

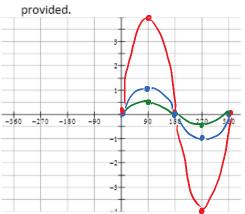
domain foell, -23° = 0 = 327°

last

Stretching/Compressing the Sine Function $y = sin \theta$

📆 Part 3: Amplitude

1. On the graphing calculator, draw the functions $y = \sin \theta$ and $y = 4 \sin \theta$. Sketch the graphs below on the grid



2. a. How do these graphs differ from each other? Calculate the amplitude for both functions

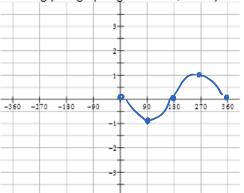
y= 4 sme is a stretch of the parent amplitude of parent = 1
amplitude of stretched = 4

b. What is the domain and range for both graphs
for 1" cycle? D= SDER, 0° ± 0 € 360° }

Rport = { yER, -1 = y = 1}

3. On your graphing calculator, draw the function y = 0.5sin θ. Sketch the graph on the same grid above.
 4. How does y=0.5sin θ differ from y = sin θ?

5. Using your graphing calculator, draw $y = -\sin \theta$. Sketch the graph below.



This one got reflected in x-axis

- storts at axis

- Hen goes down anglitude is

3. Summarize what the letter a represents in $y = a \sin \theta$ "a" controls amplitude (stretch compress)
and reflections in x-axis reported to state!

12. Fill in key characteristics of each graph.

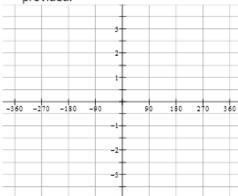
	$y = \sin \theta$	$y = 4 \sin \theta$	y = 0.5 $\sin \theta$.			
axis	0	0	0			
Max&Min	MAX=1 MN=-1	MAX=4 MM=-4	MAX=0,5 MIN=-0,5	5		
Period	360°	360°	360°			
Amplitude	1	Ч	0.5			

Where 1" and last pts occur 1" = 0° | ast = 360° | 1st = 0° | ast = 360° | 1st = 0° | ast = 360° 4. Out of all the properties (period, Max&Min, axis, amplitude, five points of cycle), which get affected by a?

MAX + MIN & get affected by "a" amplitude

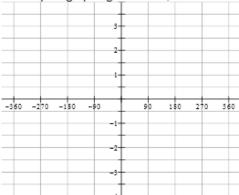
Part 4: Horizontal Stretch or Compression

5. On the graphing calculator, draw the functions $y = \sin \theta$ and $y = \sin \theta$. Sketch the graphs below on the grid provided.



6. How do these graphs differ from each other? Calculate the period for both graphs.

7. On your graphing calculator, draw the functions $y = \sin \theta$ and $y = \sin 0.5$. Sketch these graphs below.



8. How do these graphs differ from each other? Calculate the period for both graphs.

9. Summarize what the letter k represents in $y = \sin k\theta$ K stretzles compresses the function horizontally

13. Fill in key characteristics of each graph.

	$y = \sin \theta$	$y = \sin 3\theta$.	y = $\sin 0.5 \theta$.
axis			
Max&Min			
Period			
Amplitude			
Where 1 st and last pts occur			

10. Out of all the properties (period, Max&Min, axis, amplitude, five points of cycle), which get affected by k?

penod = 360° and 5 point of the cycle get affected by "k"

ignore regarives

11. Describe each equations key characteristics then sketch



a.
$$y = -3\sin(x + 45) + 1$$

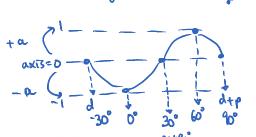
b.
$$y = \sin \frac{1}{4} (x - 60) - 1$$

c.
$$y = \sin(-3x - 90)$$

Hint: factor the k out

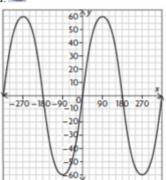
$$y=lsm(-3(x+20))+0$$

 $a=1$ $k=-3$ $d=-30$ $c=0$

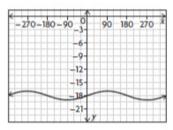


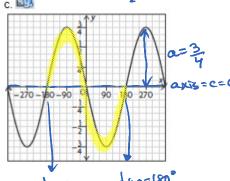
12. Find the equations for the following



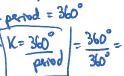


b.





9+6=180. d=-180



00 y= 3 sm[1(2+1800)]+0

WATER

AT LUCIS C. AAUC Date:	Name	
17 Unit 6 11UC Date:	Name:	

