NOTESsomeANS

Notes that are done in class will be updated online periodically

(Any questions lest blank you are responsible) to my yourself -> get help if needed.

1 U n	it 7	11U C D	ate:	Name:		
	T4-4!	TEO1	F -1-4-	Exponentials Unit		
C^~	Doft	ve IESI	date	EST mark, Overall mark now		
				you improve upon?		
	LOOKIII	g back, t	wilat call	you improve upon:		
	This ur life that of relat review expone that yo	nit introd t either g ionships exponer ents. Kee u will lea	uces you grow or d can be t nt laws fr ep in min arn in the	ng Goals I to a new type of function – the exponential function. There are many ecay at a constant rate, for example: population growth, or radioactive modelled with an exponential. Before you learn about properties of this om gr.9-10 and learn a new exponent law that allows you to work with d that this year you will not know what the inverse of the exponential is gr.12 advanced functions course – but to take this course you must take the transfer of the exponential is gr.12 advanced functions.	e decay. To s function, o rational (s, this is s	hese type , you must fraction) omething
F1	Succ	ess C	riteri	a		
300		I am <u>re</u>	ady for t	his unit if I am confident in the following review topics		
		(circle the t		good at & review the ones you left undroied before you get too far behind) ng expressions, solving equations, transformations, function notation, domain & range, e	exponent lav	vs
		l under	stand the	e new topics for this unit if I can do the practice questions in the textbo	ok/hando	uts
		(check off t	ne topics for w	hich you have finished the practice) Topics	Done?	1
			Date	Working with Positive Exponents	Dolle	
				Section 7.2 p400 #5,6,7,8,9,11 & EXTRA Handout		
				Working with Integer Exponents Section 7.3 p408 #4,7,8,9,11,12 & EXTRA Handout		
				Working with Rational Exponents & Solving for x= 2 days		
				Section 7.4 416 #7,10,11,14,15,17 & TWO EXTRA Handouts		
				If there is time – Collecting Exponential Data Handout		
				Properties of Exponentials with Graphing Calc		
				Section 7.5 p423 #1,2,4 (use graphing technology online to help you if needed)		
				Intro to Exponential Growth & Decay		
				Section 7.6 p430 #4,7,9,10,11		
				Practice Exponential Growth & Decay Section 7.7 p437 #2,3,6,8,11,		
		l am nr	epared f	or the test/evalutation if		
		_		stand the main concepts from each lesson		
			:	If not, ask other students in class to help you study or visit the peer tutoring room or ask the teacher for help or get	a private tutor	
		_	L can ex	also practice "knowledge-understanding" questions from the textbook – look for questions marked by kc kplain/communicate the ideas clearly		
		_	•	If not, practice explaining a solved question to someone else or complete the assigned journal questions		
		_		also practice "communication" questions from the textbook – look for questions marked by c		
			can a	oply these concepts in word problems If not, practice "application" questions from the textbook – look for questions marked by A		
			I did no	t just memorize steps to do for different types of questions, I understai	nd the ide	as behind
				oncept and therefore can do problems in new contexts		
			■ Lean de	If not, practice "thinking-inquiry-problem-solving" questions from the textbook – look for questions marked by $ au$ or questions independently		
			- Can d	If not, try redoing an already solved example without looking at solutions		
			I can co	omplete questions quickly and with confidence		
			l compl	If not, try timing yourself for similar type questions to see progress eted the review and/or practice test		

Corrections for the textbook answers:

2	Unit	7	11UC Date:	

Name:		
TYOU I I C.		

Working with Positive Exponents



2 1. Why do you think exponent notation was invented? Used as a shortcut for
$$5x5x5 = 5^3$$

2. Summarize the exponent laws you learned in grade 9 and provide examples.

LAW	 ■ GENERALIZATION	EXAMPLE
Multiplication $a^n \cdot a^m = a^{n+m}$	- keep bases that are the same - add their exponents	34.3= 39= 19683 don't multiply 3 and 3!
Division $\frac{a^n}{a^m} = a^{n-m}$	- Keep base that is the same - subtract exponents	$\frac{7^5}{7} = 7^4 = 2401$ don't livide 7 and 7 !!
Power of a Power $\binom{n}{a}^m = a$	- keep the base -multiply exponents	$(3^2)^5 = 3^{10} = 59 049$
Power of a Product $ (a^{x}b^{y})^{\frac{1}{2}} = a^{x^{2}}b^{y^{2}} $	- distribute exponent in ord multiply at most ONE on any base of	$(5x^6y^2)^3 = 532^8y^6 = 12521^8y^6$ without exponent
Power of a Quotient $\frac{a}{b^{y}} = \frac{a}{b^{y}}$	- distribute exponent	$\left(\frac{2x^4}{3^2y^3}\right)^{\frac{5}{2}} = \frac{26\pi^{20}}{3^{10}y^{15}} = \frac{32\pi^{10}}{59049}y^{15}$
Zero Exponent	-always equals ONE	80=)
Power of sum/Diff	NO such RULE!! - con't distribute exponent - MUST expond the Long we	$(2^3 + x)^2 (3^3 + x)(3^3 + x)$
	Linzi expan we road an	$ = 2^{6} + 2^{3}x + 2^{3}x + x^{2} $ $ = 64 + 8x + 6x + x^{2} $

Write each ex	nraccion	20.2	einale	DOWAR
WILL CACIL CY	pression	ao a	Sillidic	power

= 64 + 16x+12

4.
$$\frac{4^2}{4^3}$$

5.
$$\left(5^2\right)^3$$



Simplify 6.
$$3x^3 \cdot 4x^4$$

7.
$$\frac{8x^6}{12x^4}$$

8.
$$(3xy^3)^4$$

Simplify first then solve for x.

$$3^x = 243$$

10.
$$6^x + 5 = 221$$

11.
$$x^{2}(x^{3}) = 1024$$

$$x^{5} = |025|$$

$$|x^{3}| + |x^{2}|$$

$$|y^{5}| = |025|$$

$$|y^{5}| = |025|$$

12.
$$\left(\frac{x^{10}}{x^7}\right)^3 \div x^6 = 125$$

Working with Integer Exponents



1. Explore what negative exponents mean by filling in the table MEAN to bring the base over division line + charge

		A3	-circl terus
DIVISION	EXPAND & DIVIDE	USE EXPONENT LAW	to pos. ex
2³ ÷ 2⁵	$\frac{\cancel{2}\cancel{2}\cancel{2}\cancel{2}\cancel{2}\cancel{2}}{\cancel{2}\cancel{2}\cancel{2}\cancel$	$\frac{2^{3}}{2^{5}} = 2^{3-5} = 2^{7} 2^{-2}$: 1=2
32 ÷ 34	3.3.3 = 1	32 = 32-4 = 3-2	· 132 = 3 ⁻²
5 ÷ 5'	\$ 5.5.5 53	<u>5</u> = 5 ¹⁻⁴ = 5 ⁻³	53 = 5
104 ÷105	10-10-10-10 - 10	102 = 104-2 = 10-1	$\frac{1}{10} = 10^{-1}$
$\chi^2 \div \chi^5$	77 <u>1</u> 23	2/25 = 22-5 = 2-3 :.	73 = 2

State another way to write the following. (HINT: if a base has no exponent on it, place exponent ONE on it)

2. $3^{-2} = \frac{1}{3^2} = \frac{1}{9}$ 3. $4^{-3} = \frac{1}{4^3} = \frac{1}{64}$ 4. $\frac{1}{2^{-4}} = 2^4 = 16$

$$\boxed{0} 2. \quad 3^{-2} = \frac{1}{3^2} = \frac{1}{9}$$

3.
$$4^{-3} = \frac{1}{4^3} = \frac{1}{64}$$

4.
$$\frac{1}{2^{-4}} = 2^4 = 16$$

5.
$$2x^{-3} = 2\left(\frac{1}{2}\right)^3 = \frac{2}{2^3}$$

6.
$$\frac{3}{4^{-2}} = 3(4^2) = 3(16) = 48$$

6.
$$\frac{3}{4^{-2}} = 3(4^2) = 3(16) = 48$$
7. $\frac{3x^{-2}}{(2y)^{-1}} = \frac{3^2x^{-2}}{2^{-2}y^{-1}} = \frac{3(2)^2y^{-1}}{x^2}$

$$= \frac{6y}{x^2}$$

$$\frac{1}{6^{-1}}$$
 8. $\frac{1}{6^{-1}}$

9.
$$\left(\frac{2}{3}\right)^{4}$$

10.
$$\frac{4^{-3}}{9^{-2}}$$

11.
$$\frac{8^{-2}}{3}$$

12.
$$\frac{3}{5^{-2}}$$

13.
$$\frac{(4a)^{-1}}{5b^{-3}}$$

14. Summarize the negative exponent rule

Bring just the base with the regarder exponent over the division line bring up.

+ charge to positive exponent $a^n = \frac{1}{a^n} = \frac{1}{a^n}$



15. There will be several ways to simplify expressions, depending on what rule you start applying first. Final answers

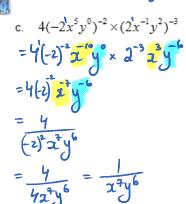
should still match no matter what route you take. To make things easier try to use the law first and regardly leaponet law first and negative

division law at the 16. Apply the laws to the following examples as you simplify the questions. Leave everything as exact numbers, with end too positive exponent answers.



a. $(4x)^2 \times 4x^2$

b. $(3d^{-3})^3 \times 3d^{-2}$



d.
$$\frac{\left(-3c^4\right)^{-2}}{c^{-1}\times\left(3c^{-2}\right)^{-2}}$$

e.
$$\left(\frac{\left(-2a^{-2}\right)^3a^3}{4a^{-4}}\right)^{-3}$$

f.
$$\frac{\left(-2xy^{3} \times 3x^{-3}y^{-2}\right)^{3}}{6x^{0}y^{-1}}$$

$$= \frac{\left(-2\right)^{3}x^{3}y^{1}\left(3\right)^{3}x^{3}y^{1}}{6x^{0}y^{-1}}$$

$$= \frac{\left(-2\right)^{3}\left(3\right)^{3}x^{3}y^{3}}{6x^{0}y^{-1}}$$

$$= \frac{\left(-2\right)^{3}\left(3\right)^{3}x^{3}y^{3}}{6x^{0}y^{-1}}$$

$$= \frac{\left(-8\right)\left(2+\right)y^{3}y^{1}}{6x^{0}}$$

$$= \frac{-216y^{4}}{6x^{0}}$$

$$= \frac{-36y^{4}}{6x^{0}}$$

Working with Rational Exponents

- 1. What does the word rational mean?

RATIONAL = FRACTION

2. Use a calculator to complete the charts

For example, to find $4^{\frac{1}{2}}$, use the sequence $4 y^x (1 + 2) =$.

To find $\sqrt[4]{16}$ use $\sqrt[3]{}$ button: either $\sqrt[16]{}$ $\sqrt[3]{}$ 4 or $\sqrt[4]{}$ $\sqrt[3]{}$ 16 try BOTH to see which way you need to remember

$4^{\frac{1}{2}} = \lambda$	² √4 = 2	16 ^{1/4} = 2	√√16 = 2
³ √27 = 3	27 ^{1/3} = 3	₹3125 = 5	3125 = 5
$216^{\frac{1}{3}} = 6$	³ √216 = 6	256 ^½ = Y	⁴ √256 = Ч
√25 == 5	$25^{\frac{1}{2}} = 6$	4 81 = 3	$81^{\frac{1}{4}} = 3$
36 ^½ =	√36 = 6	12964 = 6	∜1296 = 6

					1 10 100
а	$a^{\frac{1}{3}}$	$a^{\frac{2}{3}}$	$a^{\frac{2}{3}}$	$a^{\frac{4}{3}}$	a ten exp
8	$8^{\frac{1}{3}} = \sqrt[3]{8} = 2$	$8^{\frac{2}{3}} = \sqrt[3]{8^2} = 2^2 = 4$		8 N3 = 3 8 n = 5 n = 10	8 5 3 8 = 2 = 32
64	6413 = 364 = 4	6443 = 3/642= 42=16	64	256	1024
125	125 13 = 3 125 = 5	2.5	125	625	3125

3. Summarize the rule when the exponent is in a rational form $\frac{1}{n}$ and $\frac{m}{n}$

$$a^{\frac{m}{n}} = \sqrt{a^m}$$

 $a^{n} = \sqrt{a}$ $a^{n} = \sqrt{a}$ $a^{m} = \sqrt{a}$ -the denominator is the type of root

-the numerator is like regular exponent

the following in a different notation. Simplify if possible. brackets or exponents are not there - insert them) $a^{n} = \sqrt{a}$ -the denominator is the type of root

regular exponent

regular exponent $a^{n} = \sqrt{a}$ $a^{n} = \sqrt{a}$ -the numerator is like the numerator is the numerator is the numerator is like the numerator is lik

4. Rewrite the following in a different notation. Simplify if possible. (HINT if brackets or exponents are not there - insert them)

a.
$$6^{\frac{2}{7}} = 3$$

b.
$$\sqrt[4]{2^1x^5}$$

a.
$$6^{\frac{2}{7}} = \frac{1}{7} 6^{\frac{2}{3}}$$
b. $4\sqrt{2^{1}x^{5}}$

$$= 2^{1/4} 2^{5/4} \quad \text{or} \quad (2x^{5})^{1/4} = (3a)^{5/3}$$

$$= 3^{5/3} 0^{5/3}$$
Two if backets or exponents are not there - insert them)
$$= (16x^{1/4})^{1/4}$$

$$=$$

c.
$$\sqrt[3]{(3a)^5}$$

$$= (3a)^{5/3}$$

$$\frac{d}{16x}$$

h.
$$-125^{\frac{1}{3}}$$

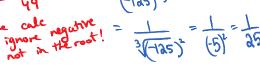
5. Write as both versions. Evaluate using the calculator for both versions, HOWEVER if you get decimals or error, use laws of exponents to simplify things first!

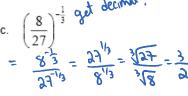


laws of exponents to simplify things first!

a.
$$-49^{\frac{1}{2}}$$
 on cale:

 $-49^{\frac{1}{2}}$ or $-49^{\frac{1}{2}}$





d.
$$\sqrt{121} =$$

e.
$$\sqrt[3]{8}$$
 =

f.
$$\sqrt[4]{16} =$$

g.
$$8^{\frac{2}{3}} =$$

h.
$$-25^{\frac{3}{2}} =$$

i.
$$81^{-\frac{3}{4}} =$$

6. Solve for x.

$$a. x^{\frac{1}{2}} = 7$$

b.
$$x^{\frac{3}{2}} = 8$$

$$\begin{array}{cccc}
 & x^{\frac{4}{5}} = 81 \\
 & x^{\frac{1}{5}} = 81 \\
 & x^{\frac{1}{5}} = 81
 \end{array}$$

$$& x^{\frac{1}{5}} = 81 \\
 & x^{\frac{1}{5}} = 81
 \end{array}$$

$$& x^{\frac{1}{5}} = 81 \\
 & x^{\frac{1}{5}} = 81
 \end{array}$$

$$& x^{\frac{1}{5}} = 81$$

$$d. x^{\frac{4}{3}} = 625$$

MORE Working with Rational Exponents & Solving for x.



1. Explain why you would get different answers for:

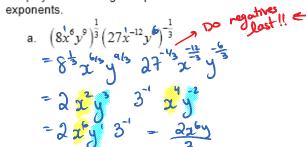
$$\sqrt[3]{(27x^4)}$$
 and $(27x)^{\frac{4}{3}}$
can insert bracket to see $(27^1x^4)^{\frac{1}{3}}$

NOT the same outside power

can insert bracket to see NOT the same our size $(27'24')^{1/3}$ 2. Explain the steps in simplifying the following. Give a reason why you can't cancel x^6 or divide 512 with 4.

$$\frac{\sqrt[3]{512x^6}}{\sqrt[3]{4x^6}}$$
 roots are different care of numerator + denom. Separately
$$\frac{512^{1/3}x^6}{\sqrt[3]{4x^6}} = \frac{8x^2}{2x^2} = 2x^{-1} = \frac{2}{x}$$

3. Simplify the following. Keep answers as exact reduced fractions and and don't leave answers with negative



b.
$$\left(\frac{64^{1}m^{15}}{343^{1}} \right)^{\frac{2}{3}} = \frac{64^{-24}3}{3^{43}} m^{\frac{-36}{3}}$$

$$= \frac{16^{-1}m^{-16}}{49^{-1}} = \frac{49}{16m^{16}}$$

c.
$$\left(256a^{12}b^{20}\right)^{\frac{3}{4}}$$

d.
$$\left(3a^{\frac{3}{2}}\right)\left(-7a^{\frac{1}{5}}\right)$$

e.
$$\left(8x^{\frac{3}{4}}y^2\right)^{-\frac{1}{3}}$$

f.
$$\frac{25x^{\frac{1}{3}}}{5x^{\frac{1}{4}}}$$

- 4. Solve the following for x.HINT: Try to make the bases match, and combine multiple bases into one single base for each side, using laws of exponents. Then do trial and error.
 - 322-5=3

32-5=0

b. $\left(\frac{1}{5}\right)^{-3x} \cdot 25^{x-1} = \frac{1}{125}$

 $(5^{3x}) 5^{2(x-1)} = 5^{-3}$

53x+21=

.. exporants one 3x+2(x-1)=-3 3x+2(x-1)=-3+2 5x=-1 x=-1=-0.2 5=-0.2 5=-0.2



 $c. 5^{4-x} = 5^x$

d. $4^x \cdot \frac{1}{16} = 2^{3x+6}$

e. $7^{2x} \cdot 7^{3-x} = 49^{x+5}$

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If there is time - Collecting Exponential Data

Eli "M" ination - Radioactive Decay of Atoms

All matter is made up of atoms. Some kinds of atoms have too much energy and are unstable. These atoms are called radioactive. It is not possible to predict exactly when a radioactive atom will release its extra energy and form a different stable atom. This process is called radioactive decay. In this experiment you will model this process

Materials

M&M or skittles for groups Paper plates or napkins Plastic containers or cups

- Pour a bag of M&M's or skittles onto a paper plate/napkin so that the candies are one layer thick so you can see if
 they have the logo in them or not. The candies represent the atoms. Count the number you have at the start and
 record in the table.
- Remove all the M&M's with the logo showing on one side these will represent atoms that have decayed. Count and record the number of M&M's remaining on the chart below.
- Pour the remaining candies into a container. Shake the container and pour these M&M's back onto the plate.
 Again remove all the M&M's with the logo showing. Continue to repeat this process until all the M&M's are removed. Add additional trial numbers to the chart below if needed.

NUMBER OF ALOMS REMAINING

4. Fill in the table and sketch the relationship.

Trial Number	Radioactive Atoms Remaining
Start with	
1	
2	
3	
4	
5	
	,

			 ,	,	,		,	,		
Si S	1 1									1
	1 1									1
1	1 1	1								1
1	1 1									1
	1 1									1
	ļ		 							.
1 1	1 1									1
	1 1									1
1	1 1									1
	1		 							************
1 1	1 1									1
3	1 1									1
	.i		 							<u>i</u>
	1 1									
i i	1 1	1								1
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1 1	1 1	1								1
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	1 1									1
1	1 1									1
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	1 1									
	1 1									1
31 3	1 1	1								1

TRIAL NUMBER

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Germs! - Exponential Growth

Materials

Certain bacteria, under the right conditions, multiply themselves. You will use strips of paper, each representing a bacterium, to model its growth. Paper Scissors

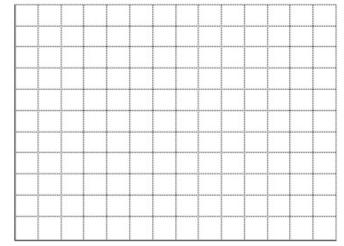
5. Cut your paper in the following arrangement based on group number you're given

	Group 1	Group 2	Group 3	Group 4	Group 5	Group 6
Pieces of paper to start with	1	2	3	1	2	3
Cut each given piece into this many equal pieces each time	2	2	2	4	4	4

6. Fill in the table and sketch the relationship.

Cuts	# of Bacteria
Start with	
1	
2	
3	
4	
5	
6	

NUMBER OF BACTERIA



7. Clean up after your group please.

OF CUTS MADE

8. What is the domain and range of the Radioactive decay question? Explain.

9. What is the domain and range of the Germs question? Explain.

Properties of Exponentials with Graphing Calculators

9

A. Complete the tables of values for the functions g(x) = x, $h(x) = x^2$ and $k(x) = 2^x$

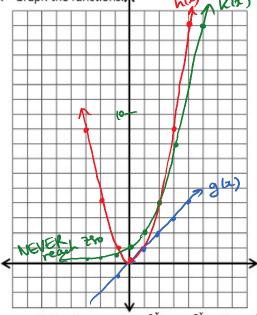
B. Calculate first and second differences. (6 RAPH) >ナ)

X	g(x)	1 st diff	2 nd diff
-3		1	1
- 2			
-1	-1		
0	0	1	
1	T.	t	
2	2	1	/
3	3	1 .	
4	4		
5	5		

X	h(x)	1 st diff	2 nd diff
- 3	9	-5	2
- 2	Ч	-3	2
-1	1	-1	2
0	0	1	2
1	1	3	2
2	4	5	2
3	9	7	2
4	طا	9	
5	25		

х	k(x)	1 st diff	2 nd diff
-3	2-3=0.125	0.125	0.125
- 2	1-5-0.52	0.25	0.25
-1	J_1 = 0.2	0.5	
0	2°= 1	l l	2
1	2'=2	2	3
2	22=4	4	4
3	8	8	8
4	16	Ь	
5	32		

C. Graph the functions.



D. Complete the chart for each function.

ER Y	t r
r ye	R, y20
ye.	R, 4>0
	R ye

E. How do the y-values change as the x-values change?

change?

linear - y-values change by adding 1

quadratiz - y-values change by squarry

exponential - y-values change by

mult. by 2.

g.

F. Graph the functions $y = 2^x$, $y = 5^x$ and $y = 10^x$ on a graphing calculator.

G. Complete the chart for each function.

	DOMAIN	RANGE	INTERCEPTS	ASYMPTOTES
$y=2^x$	aeR	yer, y > 0	x-int NONE y-int=	(0,1) Horizontal y=
$y = 5^x$	Ч	ų	ų	4
$y = 10^x$	Ŋ	Ų	li li	<i>y</i>

H. Which curve increases faster when you trace right? Which one decreases faster when you trace left?



1.12

I. Graph the functions $y = 2^x$, $y = \left(\frac{1}{2}\right)^x$ and $y = \left(\frac{1}{10}\right)^x$ on a graphing calculator.



(at)	
	1

	DOMAIN	RANGE	INTERCEPTS	ASYMPTOTES
$y = \left(\frac{1}{2}\right)^x$	ZER	yer, y>0	x: None y: (0,1)	Horit. y=0
$y = \left(\frac{1}{10}\right)^x$	Ų	Ų	7/	Ŋ

K. How do these graphs differ from $y=2^x$? These graphs decay from left to right base = $\frac{1}{2} < 1$ 2^{2} is growth base = 2 > 1

- 2
- L. What happens when the base of an exponential function is negative?

M. What type of function is $f(x) = b^x$ when b = 1?

.. Never have base = ONE

- N. Describe how the graph of an exponential function differs from the graph of a linear and quadratic function.

Linear constant rate of

Quad

O. How do the first and second differences of exponential functions differ from those of linear and quadratic differences = need y. minus prev. y. functions? How can you tell that a function is exponential?

Linear - 1st differences are the same

Quadratiz - 2rd differences are the same - but if you find

Exponential - NONE of the differences are the same - but if you find

ratios - they'll be the same Tratios = rext. y is prev. y.

P. Investigate the graphs of the exponential function $f(x) = b^x$ for various values of b, listing all similarities and differences in their features (such as domain, range, and any intercepts and asymptotes). Generalize their

features for the cases b > 1 and 0 < b < 1. Note: An asymptote is a line that a function approaches, but never reaches.

DIFFERENCES

when b > 1

when 0 < b < 1

SIMILARITIES

same domain xER same ronge yER, y > 0 same intercepts x-int NONE, y-int (0,1) same asymptote y=0

Intro to Exponential Growth & Decay



Most (but not all) real life word problems of growth or decay have a horizontal asymptote at y=0. State the general
equation for exponentials that will most often be used for exponential word problems and explain the significance of
EACH letter in the context of a word problems.

After you do question 5, come back and adjust the equation.

I-any input of dependent variable usually time c-how long it takes to grow Policay by "b"

Clarify the differences between growth factor and growth rate.

3. Summarize how to find the 'b' in the equation.

Look for special words: double b=2

half-life b=0.5

4. Set up the models for the following word problems. If not obvious, explain what each variable represents.

e. Eg

The value of the \$250 thousand cottage increases by 0.1% every month.

$$V(m) = 350000 (1+0.001)$$
or $V = 350000 (1.001)^{m}$

b. 🍱

The 40 grams of radioactive matter within a mass decays at 2% every minute.

$$G(m) = 40(1-0.02)^{m/2}$$

= $40(0.98)^{m}$

The 200 fruit fly population doubles every week.

b=3 etc.

What will the equations look like if the questions were modified as follows.

a. Th

The value of the \$250 thousand cottage increases by 0.1% every 3 weeks.

$$V(w) = 250000 (1+0.001)^{\alpha}$$

b.
The 40 grams of radioactive matter
within a mass decays at 2% every 30

$$G(t) = 40 (1-0.02)$$
 $T = 40(0.98)^{t/30}$

 The 200 fruit fly population doubles every 5 days.

Solve the following problems:

A drug's effectiveness decreases as time passes. Each hour the 250mg drug loses 5% of its effectiveness.

How effective is the drug after 150 minutes?

$$E(h) = 250(1-0.05)^{\frac{N}{1}}$$

$$ISOmin = 2.5 \text{ hr}$$

$$E(2.5) = 250(0.95)^{\frac{N}{1}}$$

$$= 250(0.8796...) = 220mq$$

Carbon-14 has a half life of 5730 years. (If no initial amount is given, assume 100% is the initial amount) Determine the % of original carbon left after 1000 years

$$C(y) = 100 (0.5)^{\frac{5}{5}+30}$$

$$= 100 [0.88606...]$$

$$= 88.6\%$$

c.
A \$1000 deposit is made at a bank that pays monthly percent, 1.5% compounded monthly [How much will you have at the end of 10 years?]

$$V(m) = 1000 (1+0.015)^{n}$$

$$10 \text{ yrs} = 120 \text{ marks}$$

$$V(120) = 1000 (1.015)^{1200}$$

$$= 1000 (5.9693...)$$

$$= 5969.32$$

- 7. The population of a bacteria culture is cut in half by an antibiotic every 30 minutes.
 - a. If the entire bacteria culture is present at 5:00 a.m., what fraction of the bacteria culture will be left at not told thow many > think 100% or 1

$$B(m) = 1 \left(\frac{1}{2}\right)^{\frac{3}{30}}$$

$$= 1 \left(\frac{1}{2}\right)^{\frac{270}{30}}$$

$$= 1 \left(\frac{1}{2}\right)^{\frac{9}{30}} = \frac{1}{512} = 0.00195 \text{ (or } 0.195\% \text{ is left)}$$

b. At what time will the bacteria culture contain $\frac{1}{128}$ of its original population?

$$\frac{1}{128} = \left(\frac{1}{2}\right)^{\frac{1}{30}}$$

$$\frac{1}{128} = \left(\frac{1}{2}\right)^{\frac{1}{30}}$$

$$\frac{1}{128} = \frac{1}{128}$$

$$\frac{1}{128} = \frac{1}{30}$$

$$\frac{210}{128} = \frac{1}{30}$$

$$\frac{210}{128} = \frac{1}{30}$$

$$\frac{210}{128} = \frac{1}{30}$$

$$\frac{210}{128} = \frac{1}{30}$$

2. 3 hrs 30 min later @ 8:30 am 8. After half an hour $\frac{1}{32}$ of a sample of a radioactive material remains. What is it's half-life?

9. An ant colony quadruples its population every month. Currently, there are 13 000 in the nest. What is the monthly growth rate of the population?

Practice Exponential Growth & Decay

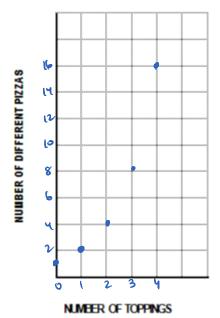
Pizza toppings

86

 Fill in the chart below by determining the different pizza's that can be created by choosing some or all or none of the available toppings

Toppings available	Different pizzas possible	# of different pizzas possible
None	plain crust with source	1
Cheese	crust or crust	2
Cheese, pepperoni	crust	4
Cheese, pepperoni, mushrooms	crust / crust	8
Cheese, pepperoni, mushrooms, bacon	rare c p m b c c c m m p c c p m m p	16

2. Sketch



3. Complete the statement:

As the number of toppings increases by 1, the number of different pizza combinations increases by 1, the number of different pizza combinations increases by 1, the number of different pizza combinations.

4. Find an equation that will model this relationship.

$$P(t) = I(a)^{t}$$

Use the equation to find how many different pizzas can be created if there are nine available toppings.

6. If the restaurant owner would like to offer 200 different pizza combinations, what is the minimum number of available toppings she would need?

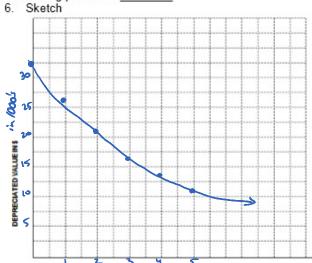
$$3^{7} = 16$$
 $2^{5} = 32$
 $2^{6} = 64$
 $2^{7} = 128$

: need at least 8 available toppings

Car Depreciation

Depreciation is the decline in a car's value over the course of its useful life. It's something new-car buyers dread. Most modern domestic vehicles typically depreciate at a rate of 15%-20% per year depending on the model of the car.

Year end	Value in \$
0	32 000
1	37000(0.80), = 52.000
2	32000 (0.80) = 30180
3	16384
4	13107-20
5	10485.76



2. Find an equation that will model this relationship.

$$V(y) = 32000 (1-0.20)^{7}$$

= 32000 (0.80)³

3. How much value does the car lose in the 1st year?

Lose \$32000 - 25600 = 6400 in the 1st year

4. How much value does the car lose in the 5th year?

13 107, 20 - 10485, 76 = 2621.44 what as much of a drap

if buy a sour car not worth to sell it with its much older...

5. After how many years will the value of the car be half of Half of 32000 = 16000 the original purchase price?

we the graph between 2-3 years ...

Radioactive Decay

8

The equation $A(t) = 100 \left(\frac{1}{2}\right)^{\frac{t}{250}}$ was used to find the present-day radioactivity of some wooden tools

at an archaeological dig.

What do all the letters and number represent?

2. Find the percent of radiation left after 1000 years

$$A(1000) = 100 \left(\frac{1}{2}\right)^{\frac{1000}{250}}$$

= 100 [0.0625]
= 6.25% of radiation is left

3. Fill in the table

Years	% of Radiation
0 2 Half life	100
250	50
500	25
750	12.5
1250	6,25
1250	3.125

4. Sketch

