

Solving Problems with Exponential Relations

% Rate, r , not same as factor, b

Example 1

To determine the equation of an exponential relationship given a rate of growth or decay as a percentage:

	a. A principal of \$500 is invested at 8% per year, compounded annually. Write an exponential equation to represent the relationship.	b. A new car costs \$20 000. Its value decreases 16% per year after it is purchased. Write an exponential equation to represent the relationship.
1. Start with the generalization for an exponential relation.	$y = ab^x$	$y = ab^x$
2. Sub in the initial amount, a .	$y = 500 b^x$	$y = 20\,000 b^x$
3. Sub in the common ratio, b . ★ for special words: • double use $b=2$ • for half-life use $b=0.5$ • for triple use $b=3$, etc ★ for Percent: • convert the percent to a decimal (divide by 100) • for growth, $b = 1+r$ • for decay, $b = 1-r$	$r = 0.08$ increase $b = 1+r$ $b = 1+0.08$ $b = 1.08$ $\therefore y = 500(1.08)^x$ value \nearrow year	$r = 0.16$ decrease $b = 1-r$ $b = 1-0.16$ $b = 0.84$ $\therefore y = 20\,000(0.84)^x$ value \nearrow year

Example 2

The population of Alberta between 1987 and 2005 can be modelled by an exponential equation. The population in 1987 was 2.4 million and the growth rate was 1.7%.

a. Write an equation to model the situation.

$a = 2\,400\,000$

$r = 0.017$
 $b = 1+r$
 $b = 1+0.017$
 $b = 1.017$

$\therefore y = ab^x$
 $y = 2\,400\,000(1.017)^x$
 population \nearrow year

b. Use your model to calculate the population in 1985.

$x = -2$ (2 yrs. back from 1987)
 $y = 2\,400\,000(1.017)^{-2}$
 $y = 2\,320\,435$ people

c. Use your model to calculate the population in 2012.

$\frac{2012}{-1987}$
 25 years
 $y = 2\,400\,000(1.017)^{25}$
 $y = 3\,657\,927$ people